

# Workshop on Verification of Autonomous Systems

## Techniques for Practical Verification

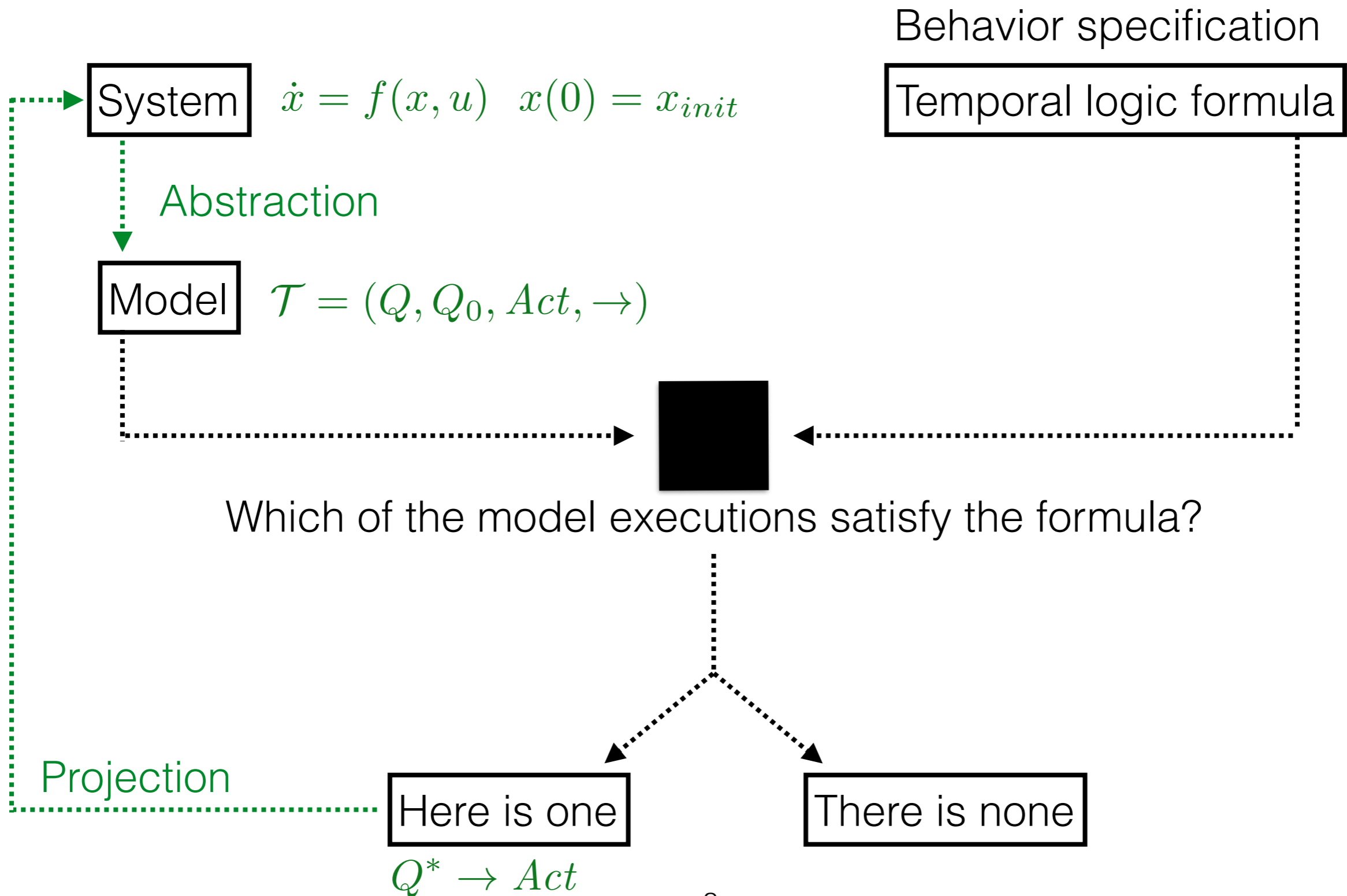
Jana Tumova



# Research interests

- Past
  - Parallel and distributed probabilistic model checking
  - Quantitative model checking of systems with degradation
  - Temporal logic analysis and control of piecewise affine systems
- Ongoing
  - Model checking-based robot motion and action planning
  - Model checking-based multi-agent control

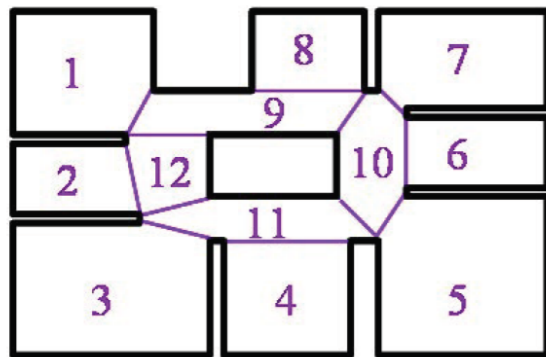
# Model checking-based planning



# Model checking-based robot mission and motion planning

## System

$$\dot{p}(t) = u(t) \quad p(t) \in P \subseteq \mathbb{R}^2 \quad u(t) \in U \subseteq \mathbb{R}^2$$
$$p(0) = P_1$$



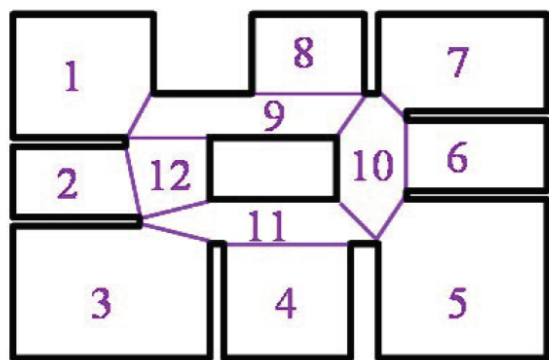
## Behavior specification

Periodically visit  $P_1, P_4, P_8$   
and never enter  $P_{10}$

# Model checking-based robot mission and motion planning

## System

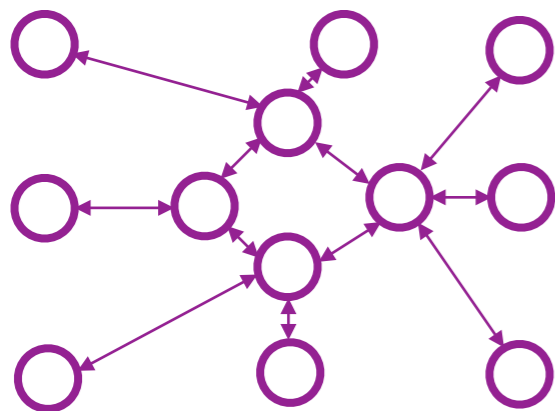
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## Behavior specification

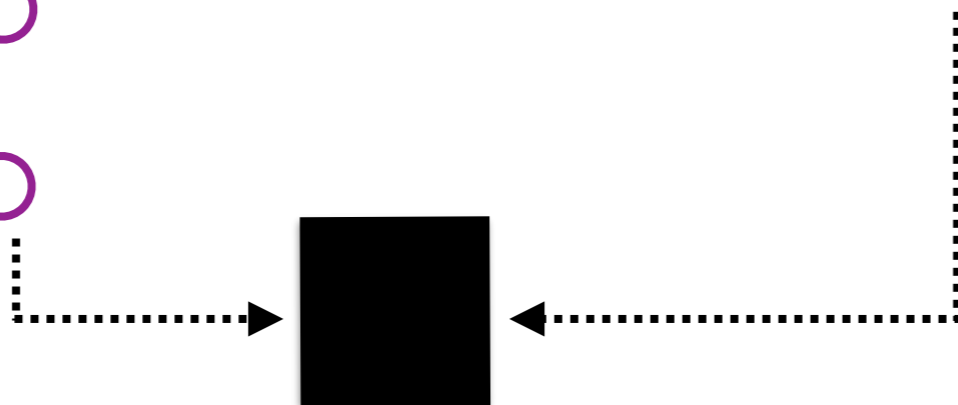
Periodically visit  $P_1, P_4, P_8$   
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## Model



## Linear Temporal Logic (LTL) formula

$$\mathcal{G}\mathcal{F} P_1 \wedge \mathcal{G}\mathcal{F} P_4 \wedge \mathcal{G}\mathcal{F} P_8 \wedge \mathcal{G} \neg P_{10}$$

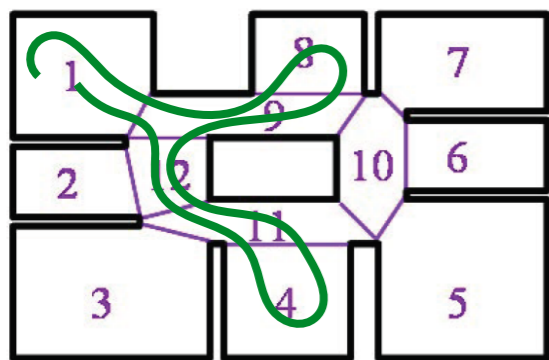


# Model checking-based robot mission and motion planning

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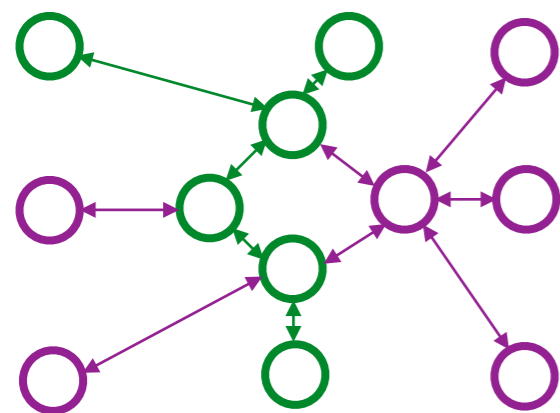
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## Behavior specification

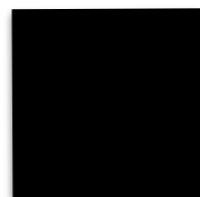
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## Model



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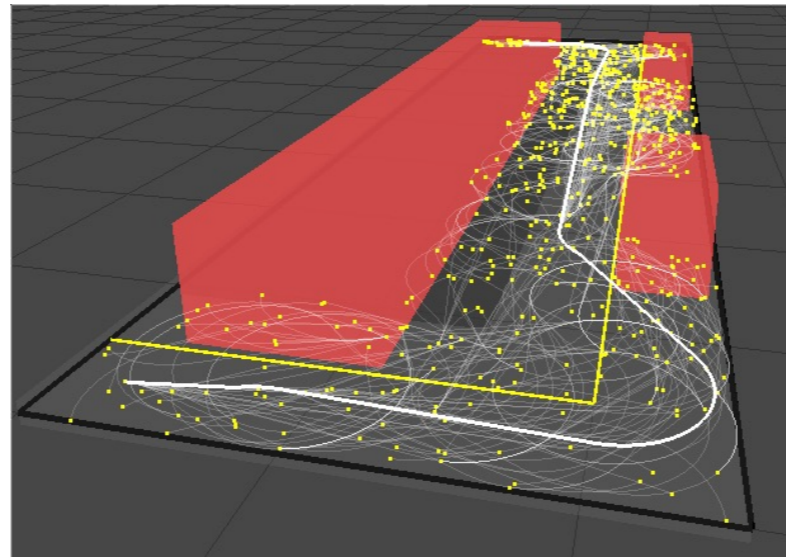
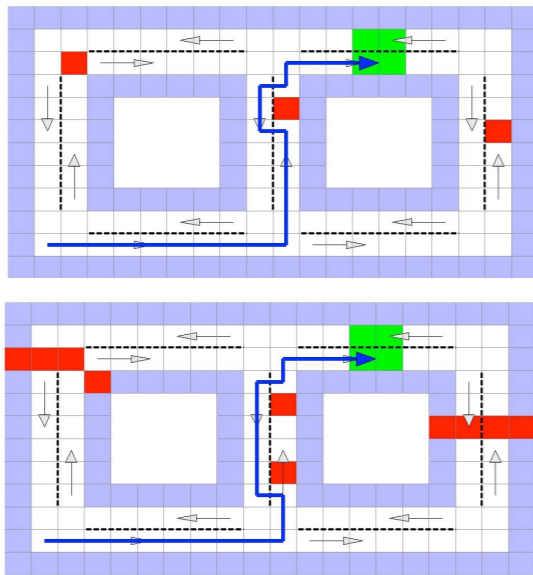
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# Research challenges

- Input user-friendliness
  - structured English, graphical representation
- Computational complexity and scalability
  - receding horizon, fragments of logics
- Dynamic environments and imprecisions of sensors and actuators
  - nondeterministic, probabilistic, partial observable models
  - reactive re-planning
- Multi-agent systems
  - task decomposition, decentralized planning
- Optimality
  - weighted models
- Specification infeasibility
  - least-violating planning, model repair, analysis of reasons

# 1 Highlight: Least violating sampling-based motion planning algorithm



[Least-violating Control Strategy Synthesis with Safety Rules](#)

in HSCC 2013, with Gavin Hall, Sertac Karaman, Emilio Frazzoli, Daniela Rus

[Incremental Sampling-based Algorithm for Minimum-violation Motion Planning](#)

in CDC 2013, with Luis Reyes-Castro, Pratik Chaudhari, Sertac Karaman, Emilio Frazzoli, Daniela Rus